

Algebra II (2yr) Review 7.1 -7.3

Simplify and do not use negative exponents

1. $(x^3y^6)(x^4y^8) = x^7y^{14}$

2. $(3x^4y^{-5}z^2)^2 = 9x^8y^{-10}z^4 = \frac{9x^8z^4}{y^{10}}$

3. $\frac{x^5y^4z^3}{xy^7z^3} = x^4y^{-3} = \frac{x}{y^3}$

4. $(xy)^0 = 1$

Find the real-number root.

5. $\sqrt{-2.89} = 1.7$

6. $\sqrt{2.25} = 1.5$

7. $\sqrt[3]{-\frac{27}{64}} = \frac{-3}{4}$ $\frac{\sqrt[3]{-27}}{\sqrt[3]{64}}$

8. Find all the real fourth roots of $\frac{625}{1296}$. $\pm \frac{5}{6}$

9. Find all the real square roots of $-\frac{25}{36}$. $\pm \frac{5}{6}$

Simplify the radical expression.

10. $\sqrt[4]{81x^{12}y^24}$ $3x^3y^6$

11. $\sqrt[2]{121g^{10}}$ $11g^5$

12. Simplify $\sqrt[3]{-27a^{10}b^6}$. $-3a^3b^2\sqrt[3]{a^1}$

13. Multiply and simplify if possible.
 $\sqrt{20} \cdot \sqrt{2} = \sqrt{40} = \sqrt{4 \cdot 10} = 2\sqrt{10}$

$$\sqrt{20} \cdot \sqrt{2} = 2\sqrt{5} \cdot \sqrt{2} \\ (2 \cdot 2) \quad 2\sqrt{10}$$

14. Multiply and simplify
 $\sqrt[3]{9x^4} \cdot \sqrt[3]{3x^7}$

Divide and simplify.

15. $\frac{\sqrt[3]{270}}{\sqrt[3]{5}} = \sqrt[3]{54} = \sqrt[3]{3 \cdot 3 \cdot 3 \cdot 2}$

$$\begin{array}{c} 5 \\ \swarrow \searrow \\ 3 \quad 3 \end{array}$$

16. Divide and simplify if possible.

$$\frac{\sqrt{84x^{28}}}{\sqrt{7x^2}} = \sqrt{12x^{26}} = \sqrt{2 \cdot 2 \cdot 3 \cdot x^{26}}$$

$$\begin{array}{c} 2 \quad 12 \\ \swarrow \searrow \\ 2 \quad 3 \end{array}$$

17. Simplify by adding or subtracting, if possible.

$$2\sqrt{2a} - 5\sqrt{2a}$$

$$-3\sqrt{2a}$$

18. Simplify by adding or subtracting, if possible.

$$2\sqrt{8x} + 6\sqrt{2x}$$

$$2\sqrt{2 \cdot 2 \cdot 2x} + 6\sqrt{2x} \rightarrow 4\sqrt{2} + 6\sqrt{2x} = 10\sqrt{2x}$$

Add or subtract if possible.

19. $4\sqrt{3} - 3\sqrt{5}$ same

20. Simplify by adding or subtracting, if possible.

$$-\sqrt{7} - 6\sqrt{16} - 4\sqrt{7}$$

$$-1\cancel{\sqrt{7}} - (6 \cdot 4) - 4\sqrt{7}$$

$$-5\sqrt{7} - 24$$

21. Multiply. $(-7 - \sqrt{5})(-2 + \sqrt{5}) = 14 - 7\sqrt{5} + 2\sqrt{5} - 5$

$$9 - 5\sqrt{5}$$

22. Multiply.

$$(6 - \sqrt{2})(-6 - \sqrt{2}) = 36 + 6\sqrt{2} + 6\sqrt{2} + 2$$

$$38 + 12\sqrt{2}$$

23. Multiply.

$$(\sqrt{7} + \sqrt{2})(\sqrt{7} - \sqrt{2}) = 7 - \sqrt{14} + \sqrt{14} - 2 = 5$$

conjugate

24. Rationalize the denominator.

$$\left(\frac{\sqrt{3x^{11}y^{11}}}{\sqrt{7x^5y^6}} \right) \left(\frac{\sqrt{7x^5y^6}}{\sqrt{7x^5y^6}} \right) = \frac{\sqrt{21x^{16}y^{17}}}{7x^5y^6} = \frac{x^3y^3\sqrt{21}y}{7x^5y^6} = \frac{x^3y^2\sqrt{21}y}{7}$$

or

$$\left(\frac{\sqrt{3x^6y^5}}{\sqrt{7}} \right) \left(\frac{\sqrt{7}}{\sqrt{7}} \right) = \frac{\sqrt{21x^6y^5}}{7} = \frac{x^3y^2\sqrt{21}y}{7}$$

Rationalize the denominator of the expression. Assume that all variables are positive.

25. $\left(\frac{\sqrt{2} - \sqrt{5}}{\sqrt{2} + \sqrt{5}} \right) \left(\frac{\sqrt{2} - \sqrt{5}}{\sqrt{2} - \sqrt{5}} \right) = \frac{2 - \sqrt{10} - \sqrt{10} + 5}{2 - \sqrt{10} + \sqrt{10} - 5} = \frac{7 - 2\sqrt{10}}{-3}$